

FINALTERM EXAMINATION
Spring 2010
CS502- Fundamentals of Algorithms (Session - 4)
Time: 90 min
Marks: 58

Question No: 1 (Marks: 1) - Please choose one

An optimization problem is one in which you want to find,

- ▶ Not a solution
- ▶ An algorithm
- ▶ Good solution
- ▶ **The best solution**

Question No: 2 (Marks: 1) - Please choose one

Although it requires more complicated data structures, Prim's algorithm for a minimum spanning tree is better than Kruskal's when the graph has a large number of vertices.

- ▶ **True**
- ▶ False

Question No: 3 (Marks: 1) - Please choose one

If a problem is in NP, it must also be in P.

- ▶ **True**
- ▶ False
- ▶ unknown

Question No: 4 (Marks: 1) - Please choose one

What is generally true of Adjacency List and Adjacency Matrix representations of graphs?

- ▶ *Lists* require less space than *matrices* but take longer to find the weight of an edge (v_1, v_2)
- ▶ ***Lists* require less space than *matrices* and they are faster to find the weight of an edge (v_1, v_2)**

- ▶ *Lists* require more space than *matrices* and they take longer to find the weight of an edge (v_1, v_2)
- ▶ *Lists* require more space than *matrices* but are faster to find the weight of an edge (v_1, v_2)

Question No: 5 (Marks: 1) - Please choose one

If a graph has v vertices and e edges then to obtain a spanning tree we have to delete

- ▶ v edges.
- ▶ $v - e + 5$ edges
- ▶ $v + e$ edges.
- ▶ **None of these**

Question No: 6 (Marks: 1) - Please choose one

Maximum number of vertices in a Directed Graph may be $|V^2|$

- ▶ **True**
- ▶ False

Question No: 7 (Marks: 1) - Please choose one

The Huffman algorithm finds a (n) _____ solution.

- ▶ **Optimal**
- ▶ Non-optimal
- ▶ Exponential
- ▶ Polynomial

Question No: 8 (Marks: 1) - Please choose one

The Huffman algorithm finds an exponential solution

- ▶ True
- ▶ **False**

Question No: 9 (Marks: 1) - Please choose one

The Huffman algorithm finds a polynomial solution

- ▶ True
- ▶ **False**

Question No: 10 (Marks: 1) - Please choose one

The greedy part of the Huffman encoding algorithm is to first find two nodes with **larger** frequency.

- ▶ True
- ▶ **False**

Question No: 11 (Marks: 1) - Please choose one

The codeword assigned to characters by the Huffman algorithm have the property that no codeword is the postfix of any other.

- ▶ True
- ▶ **False**

Question No: 12 (Marks: 1) - Please choose one

Huffman algorithm uses a greedy approach to generate a postfix code T that minimizes the expected length $B(T)$ of the encoded string.

- ▶ True
- ▶ **False**

Question No: 13 (Marks: 1) - Please choose one

Shortest path problems can be solved efficiently by modeling the road map as a graph.

- ▶ **True**
- ▶ False

Question No: 14 (Marks: 1) - Please choose one

Dijkstra's single source shortest path algorithm works if all edges weights are non-negative and there are negative cost cycles.

- ▶ True
- ▶ **False**

Question No: 15 (Marks: 1) - Please choose one

Bellman-Ford allows negative weights edges and negative cost cycles.

- ▶ True
- ▶ **False**

Question No: 16 (Marks: 1) - Please choose one

The term "coloring" came form the original application

which was in architectural design.

- ▶ True
- ▶ False

Question No: 17 (Marks: 1) - Please choose one

In the clique cover problem, for two vertices to be in the same group, they must be adjacent to each other.

- ▶ True
- ▶ False

Question No: 18 (Marks: 1) - Please choose one

Dijkstra's algorithm is operates by maintaining a subset of vertices

- ▶ True
- ▶ False

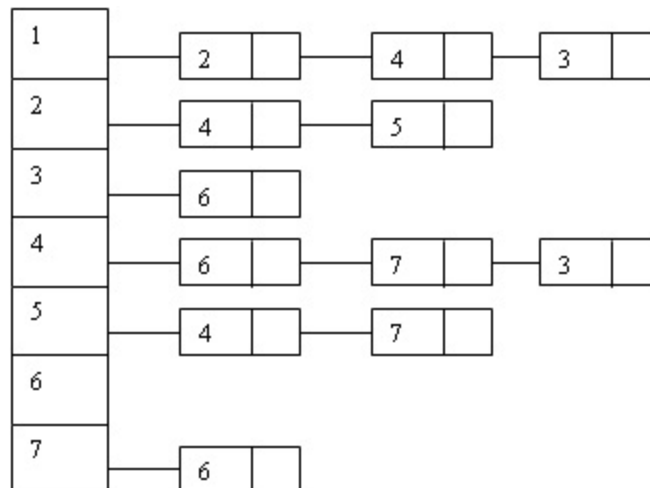
Question No: 19 (Marks: 1) - Please choose one

The difference between Prim's algorithm and Dijkstra's algorithm is that Dijkstra's algorithm uses a different key.

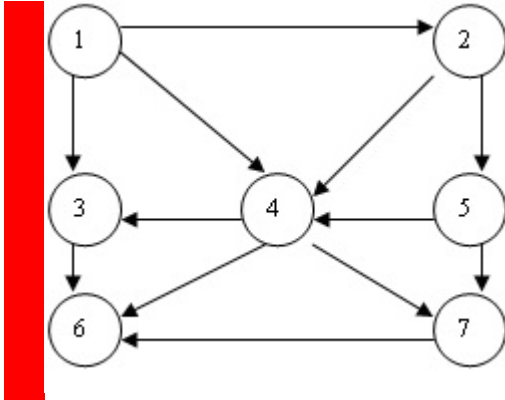
- ▶ True
- ▶ False

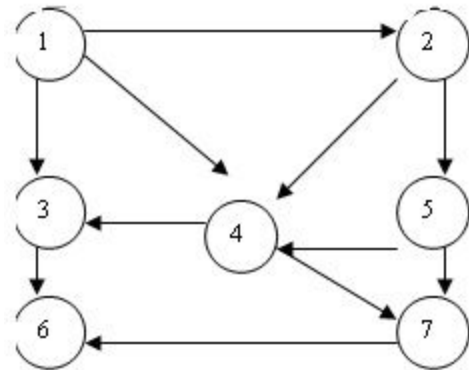
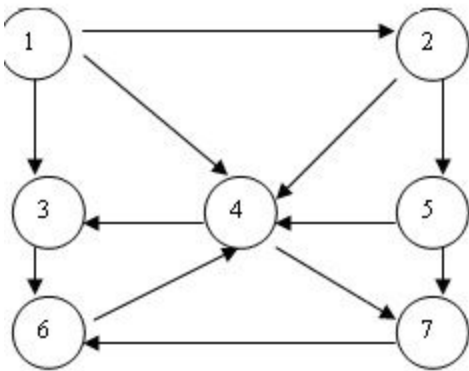
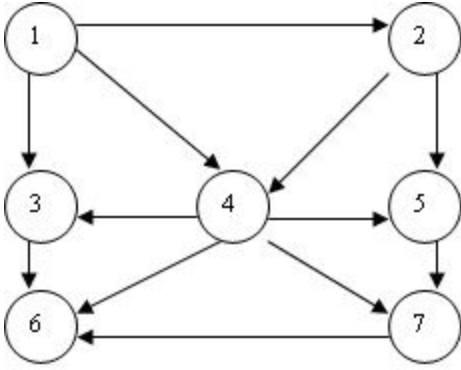
Question No: 20 (Marks: 1) - Please choose one

Consider the following adjacency list:



Which of the following graph(s) describe(s) the above adjacency list?





Question No: 21 (Marks: 1) - Please choose one

We do sorting to,

- ▶ keep elements in random positions
- ▶ keep the algorithm run in linear order
- ▶ keep the algorithm run in $(\log n)$ order
- ▶ keep elements in increasing or decreasing order

Question No: 22 (Marks: 1) - Please choose one

After partitioning array in Quick sort, pivot is placed in a position such that

- ▶ Values smaller than pivot are on left and larger than pivot are on right
- ▶ Values larger than pivot are on left and smaller than pivot are on right
- ▶ Pivot is the first element of array
- ▶ Pivot is the last element of array

Question No: 23 (Marks: 1) - Please choose one

Merge sort is stable sort, but not an in-place algorithm

- ▶ True
- ▶ False

Question No: 24 (Marks: 1) - Please choose one

In counting sort, once we know the ranks, we simply _____ numbers to their final positions in an output array.

- ▶ Delete
- ▶ copy
- ▶ Mark
- ▶ arrange

Question No: 25 (Marks: 1) - Please choose one

Dynamic programming algorithms need to store the results of intermediate sub-problems.

- ▶ True
- ▶ False

Question No: 26 (Marks: 1) - Please choose one

A $p \times q$ matrix A can be multiplied with a $q \times r$ matrix B. The result will be a $p \times r$ matrix C. There are $(p \cdot r)$ total

entries in C and each takes _____ to compute.

- ▶ $O(q)$
- ▶ $O(1)$
- ▶ $O(n^2)$
- ▶ $O(n^3)$

Question No: 27 (Marks: 2)

Give a detailed example for 2-d maxima problem.

Question No: 28 (Marks: 2)

Differentiate between back edge and forward edge.

Question No: 29 (Marks: 2)

How the generic greedy algorithm operates in minimum spanning tree?

Question No: 30 (Marks: 2)

What are two cases for computing $d^{(k-1)}$ assuming we already have the previous matrix $d^{(k-1)}$ using Floyd-Warshall algorithm?

Question No: 31 (Marks: 3)

Describe Minimum Spanning Trees Problem with examples.

Question No: 32 (Marks: 3)

What is decision problem, also explain with example?

Question No: 33 (Marks: 3)

Prove that the generic TRAVERSE (S) marks every vertex in any connected graph exactly once and the set of edges $(v, \text{parent}(v))$ with $\text{parent}(v) \in S$ form a spanning tree of the graph.

Question No: 34 (Marks: 5)

Suppose you could reduce an NP-complete problem to a polynomial time problem in polynomial time. What would be the consequence?

Question No: 35 (Marks: 5)

Prove the following lemma,

Lemma: Given a digraph $G = (V, E)$, consider any DFS forest of G and consider any edge $(u, v) \in E$. If this edge is a tree, forward or cross edge, then $f[u] > f[v]$. If this edge is a back edge, then $f[u] < f[v]$.

Question No: 36 (Marks: 5)

What is the cost of the following graph?

